

Learning a Static Analyzer from Data



Pavol Bielik



Veselin Raychev



Martin Vechev



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Department of Computer Science
ETH Zurich

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Writing a Static Analyzer

DOOP

Framework for Java
Pointer Analysis



17 contributors

TAJS

Static Type Checker
for JavaScript



Static Type Checker
for JavaScript



~400 contributors

Writing static analyzer is



Writing static analyzer is **hard**

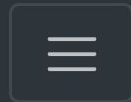
Writing static analyzer is **frustrating**

Writing static analyzer is **time consuming**

Writing static analyzer is **brittle**

[Learn more](#)

Example of Unsound Analysis



```
1 /* @flow */
2
3 var data = [7, 2, 9];
4
5 function collect(val, idx, obj) {
6   if (val > this.threshold) { Missed Error
7
8   }
9 }
10
11 data.threshold; Error correctly reported
12 data.forEach(collect);
```

Errors

JSON

AST

v0.51.0 ▼

```
11: data.threshold;
      ^ property `threshold`. Property not found in
11: data.threshold;
      ^ Array
```

Can we learn a static analyzer?
(aka its abstract transformers)

This Work: Learn Static Analyzer from Data

Input Dataset

$$\mathcal{D} = \{\langle x^j, y^j \rangle\}_{j=1}$$

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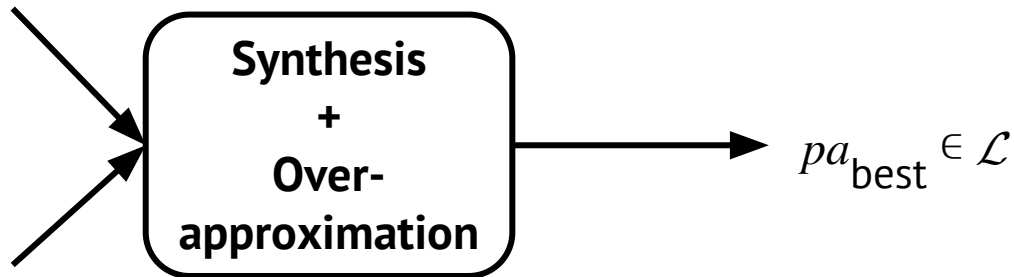
Language \mathcal{L}

*for abstract
transformers*

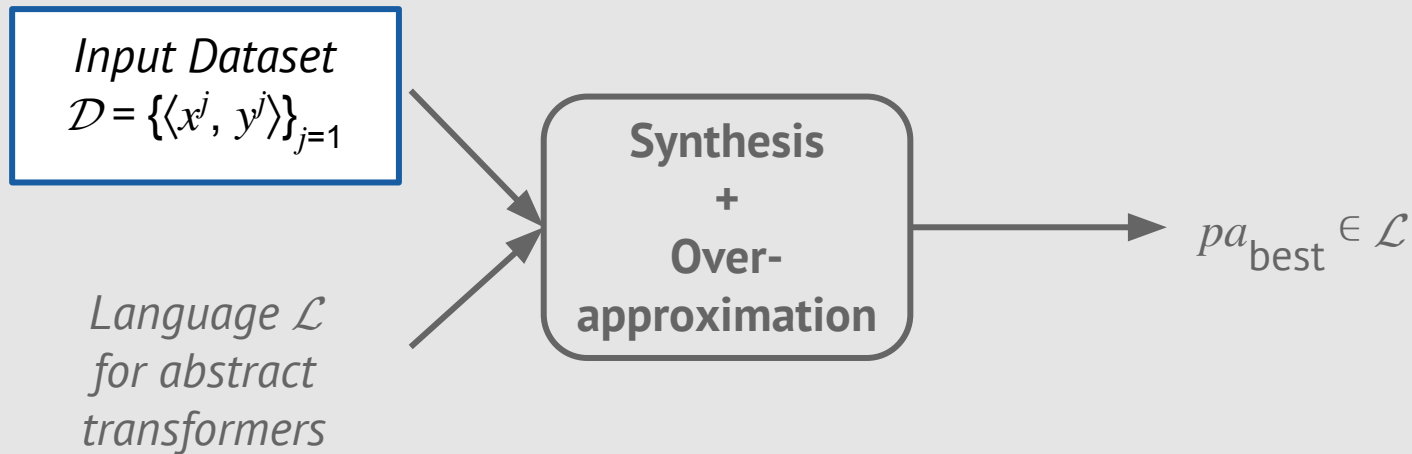
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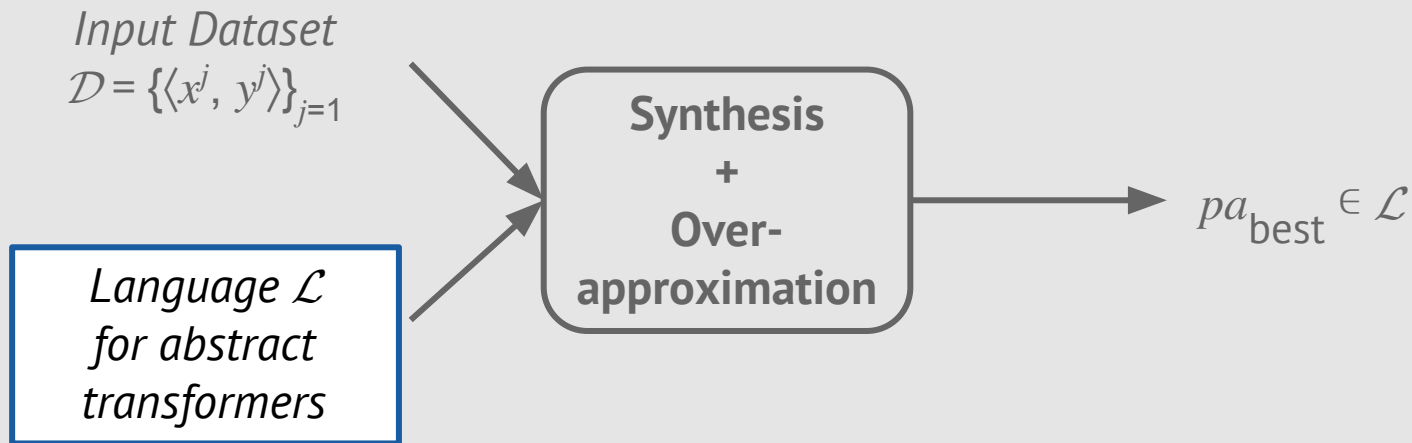


This Work: Learn Static Analyzer from Data



How to obtain suitable dataset?

This Work: Learn Static Analyzer from Data

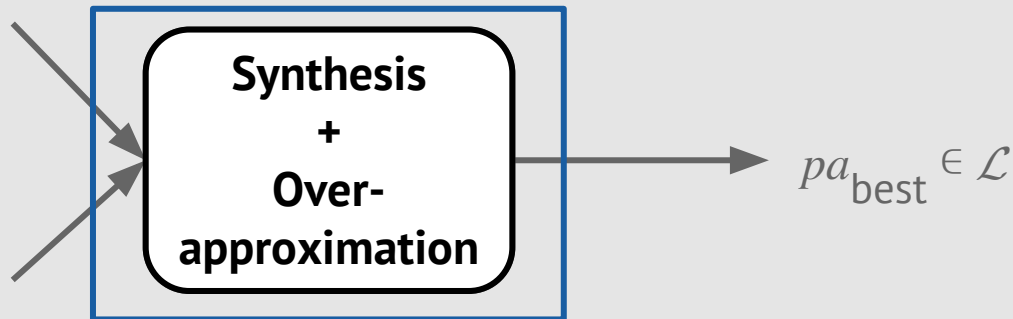


**What is the language over which to learn?
How to allow generating new interesting transformers?**

This Work: Learn Static Analyzer from Data

Input Dataset
 $\mathcal{D} = \{\langle x^j, y^j \rangle\}_{j=1}$

Language \mathcal{L}
for abstract
transformers



How to design scalable learning over large search spaces?
How to prevent overfitting?

Can we learn a static analyzer?

interpretable and sound



Can we learn a static analyzer?

Problem Formulation

$$pa_{\text{best}} = \arg \min_{pa \in \mathcal{L}} cost(\mathcal{D}, pa) \quad \leftarrow \text{analysis precision}$$

analysis soundness \rightarrow st. $\forall \langle x, y \rangle \in \mathcal{D} . \alpha(y) \sqsubseteq pa(x)$

An Example Transformer Learned

```
Array.prototype.filter ::=
  if caller has one argument then
    points-to global object
  else if 2nd argument is Identifier then
    if 2nd argument is undefined then
      points-to global object
    else
      points-to 2nd argument
  else if 2nd argument is this then
    points-to 2nd argument
  else if 2nd argument is null then
    points-to global object
  else //2nd argument is a primitive value
    points-to new allocation site
```

An Example Transformer Learned

```
Array.prototype.filter ::=  
  if caller has one argument then  
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  else if 2nd argument is Identifier then  
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An Example Transformer Learned

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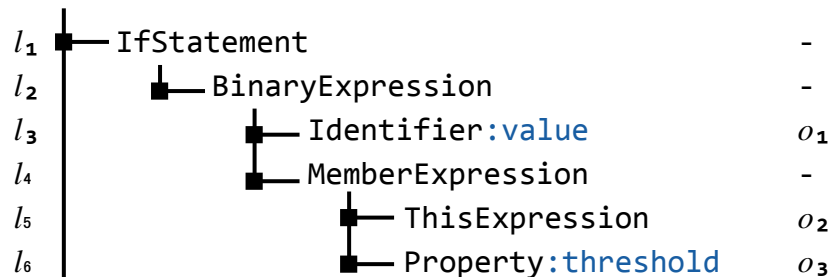
***Let us show the learning on an example analysis
(aka points-to analysis)***

Dataset: Points-to Analysis

Program

```
function collect(value, idx, obj) {  
  if (value >= this.threshold) {  
    ...  
  }  
  ...  
}
```

Abstract Syntax Tree (AST)



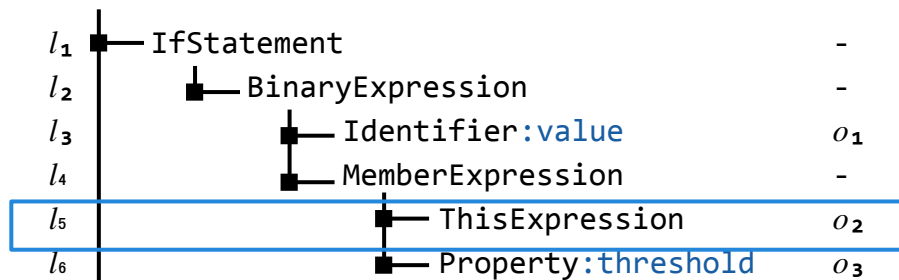
*execution
reads/writes*

Dataset: Points-to Analysis

Program

```
function collect(value, idx, obj) {  
  if (value >= this.threshold) {  
    ...  
  }  
  ...  
}
```

Abstract Syntax Tree (AST)



$\langle (AST, l_5), o_2 \rangle$

$$\mathcal{D} = \{ \langle \hat{x}^j, \hat{y}^j \rangle \}_{j=1}$$

Language Describing Abstract Transformers

$$l \in \mathcal{L} := a \mid \text{if } g \text{ then } l \text{ else } l$$
 $a \in \text{Actions}$ $g \in \text{Guards}$

```
function collect(val, idx, obj) {  
  if (val >= this.threshold) { ... }  
}
```

Points-to Query

```
var dat = [5, 3, 9];  
dat.filter( collect, ctx );
```

↑
method name
is filter

 g_1

↑
has
2nd argument

 g_2

Language Describing Abstract Transformers

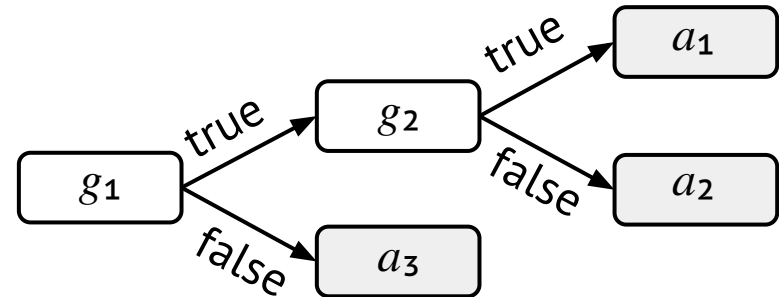
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var dat = [5, 3, 9];  
dat.filter( collect, ctx );
```

Points-to Query

a_1

method name has
is filter 2nd argument
 g_1 g_2



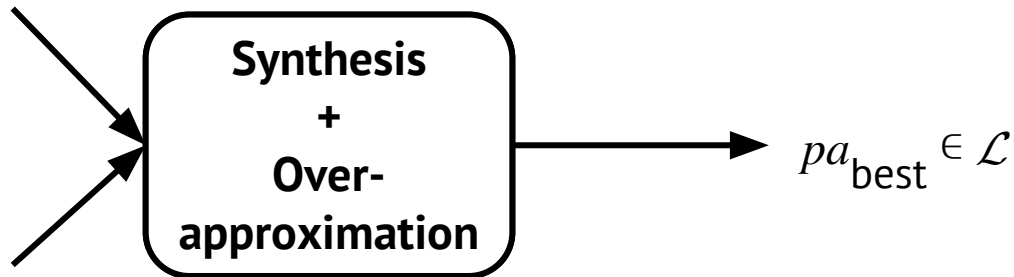
can be represented as decision tree

paths interpreted as abstract transformers

Learning: Decision Trees

Input Dataset
 $\mathcal{D} = \{\langle x^j, y^j \rangle\}_{j=1}$

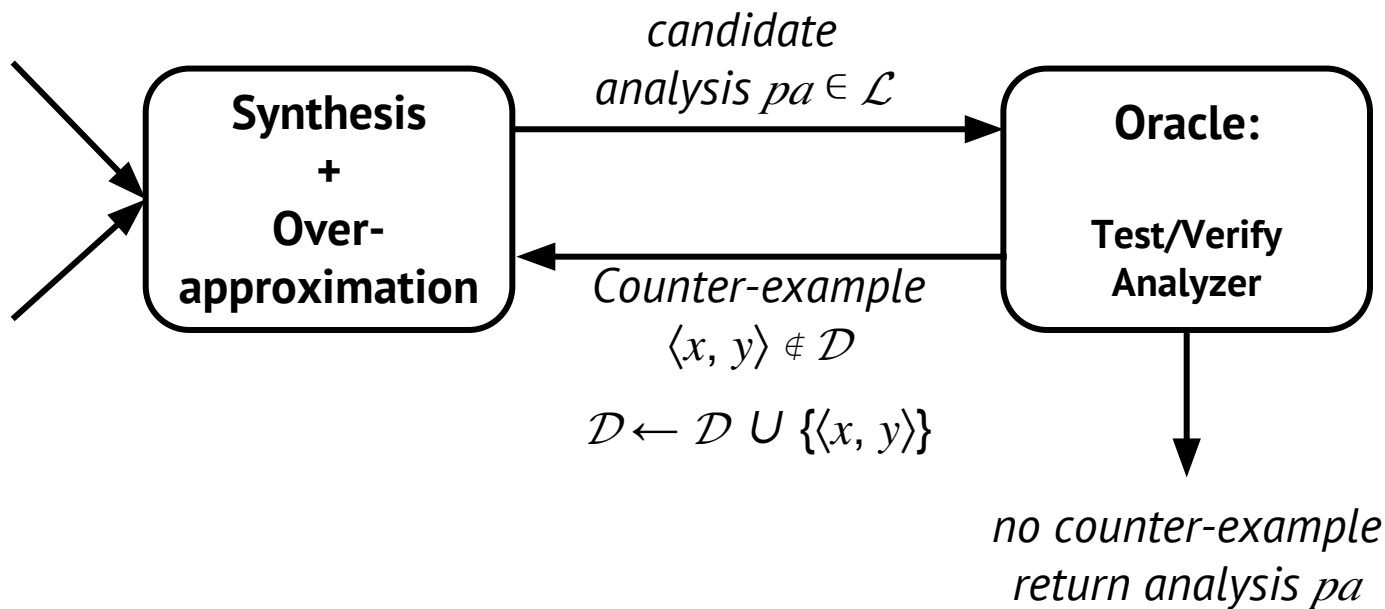
*Language \mathcal{L}
for abstract
transformers*



Learning: Decision Trees + CEGIS

Input Dataset
 $\mathcal{D} = \{\langle x^j, y^j \rangle\}_{j=1}$

Language \mathcal{L}
for abstract
transformers



Learning: Problem Formulation

Problem Formulation

$$pa_{\text{best}} = \arg \min_{pa \in \mathcal{L}} \text{cost}(\mathcal{D}, pa)$$

$$\text{st. } \forall \langle x, y \rangle \in \mathcal{D} . \alpha(y) \sqsubseteq pa(x)$$

guarantees analysis soundness

Cost Function

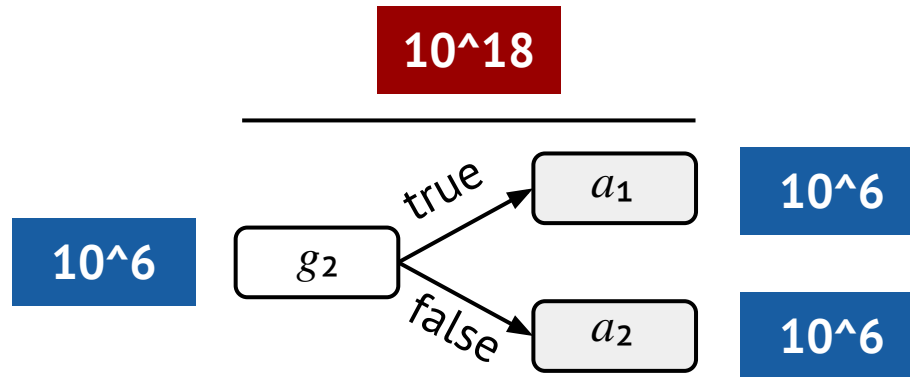
$$r(x, y, pa) = \text{if } (y \neq pa(x)) \text{ then } 1 \text{ else } 0$$

$$\text{cost}(\mathcal{D}, pa) = \sum_{\langle x, y \rangle \in \mathcal{D}} r(x, y, pa)$$

prefer analysis with fewer errors

Learning Algorithm

$l \in \mathcal{L} := a \mid \text{if } g \text{ then } l \text{ else } l$

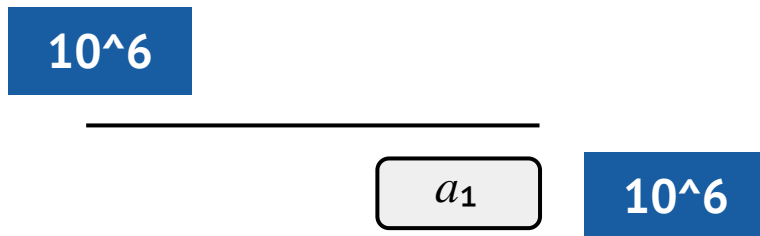


Untractable

Learning Algorithm

$l \in \mathcal{L} := a \mid \text{if } g \text{ then } l \text{ else } l$

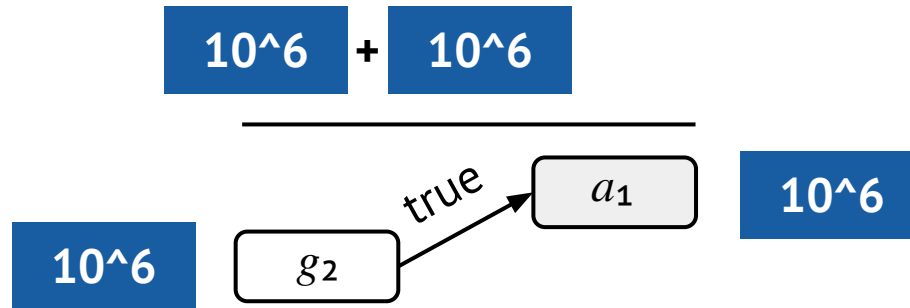
Key Idea: Synthesise Programs in Parts



Learning Algorithm

$$l \in \mathcal{L} := a \mid \text{if } g \text{ then } l \text{ else } l$$

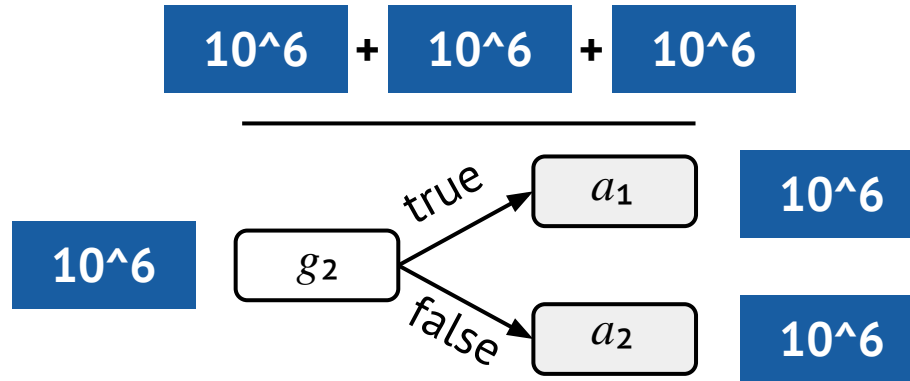
Key Idea: Synthesise Programs in Parts



Learning Algorithm

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Key Idea: Synthesise Programs in Parts

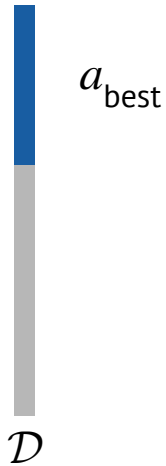


Learning Algorithm

$$a_{\text{best}} = \arg \min_{a \in \text{Actions}} \text{cost}(\mathcal{D}, a)$$

$$\text{cost}(\mathcal{D}, a_{\text{best}}) > 0$$

refine analysis



$$\text{cost}(\mathcal{D}, a_{\text{best}}) = 0$$

a_{best}

no errors
return a_{best}



Learning Algorithm

$$g_{\text{best}} = \arg \max_{g \in \text{Guards}} \text{InfGain}(\mathcal{D}, g, a_{\text{best}})$$

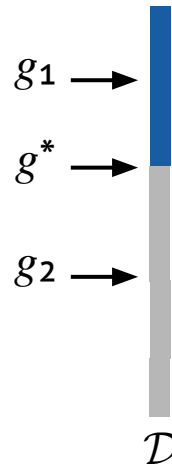
$$\text{cost}(\mathcal{D}, a_{\text{best}}) > 0$$

refine analysis



Find split
that separates

a_{best}



Learning Algorithm

$$g_{\text{best}} = \arg \max_{g \in \text{Guards}} \text{InfGain}(\mathcal{D}, g, a_{\text{best}})$$

$$\text{cost}(\mathcal{D}, a_{\text{best}}) > 0$$

a_{best}

refine analysis



Find split
that separates

a_{best}

$g_1 \rightarrow$

$g^* \rightarrow$

$g_2 \rightarrow$



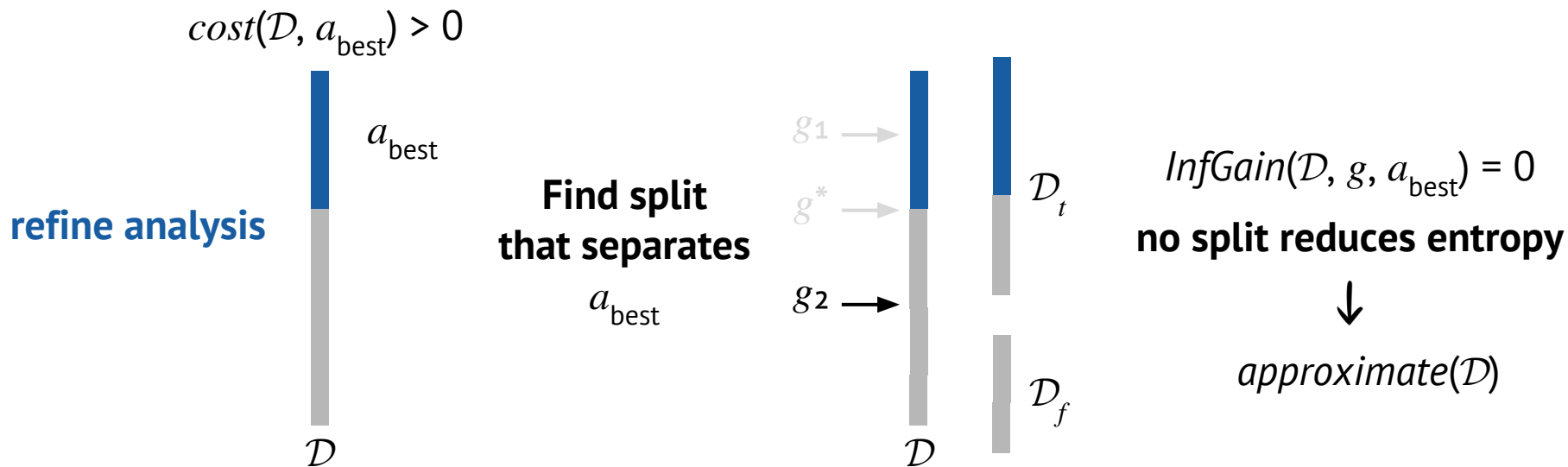
\mathcal{D}_t

\mathcal{D}_f



Learning Algorithm

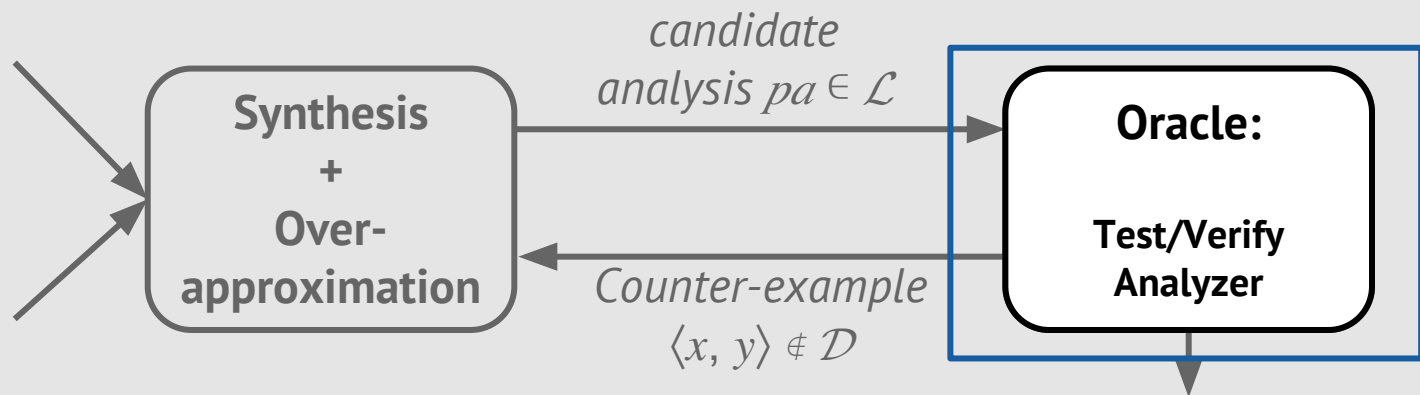
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Learning: Decision Trees + CEGIS

Input Dataset
 $\mathcal{D} = \{\langle x^j, y^j \rangle\}_{j=1}$

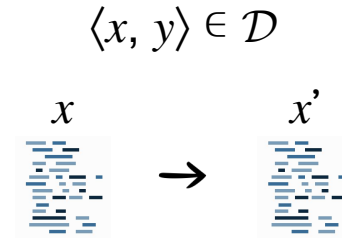
Language \mathcal{L}
for abstract
transformers



How to find complex counter-examples quickly?
How to efficiently explore hard to find corner cases?

Naive Approach: Random Fuzzing

1. Pick a random training example
2. Mutate the input randomly
3. Obtain the correct label
4. Check for correctness
5. Repeat



Execute x' \rightarrow \mathcal{D}'

$$\forall \langle x, y \rangle \in \mathcal{D}' . \alpha(y) \sqsubseteq pa(x)$$

Naive Approach: Random Fuzzing

1. Pick a random training example
2. Mutate the input randomly
3. Obtain the correct label
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5. Repeat

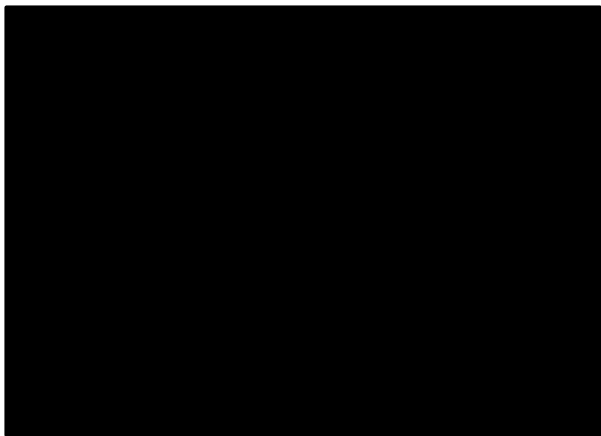
Exponential Number
of Choices

Slow

When to stop?

The Oracle: Testing an Analyzer

Key Idea: Take advantage of candidate analysis pa

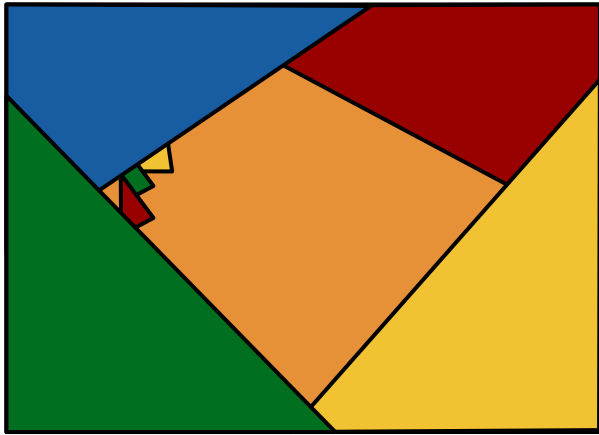


\mathcal{T}

**How to sample from
space of all programs?**

The Oracle: Testing an Analyzer

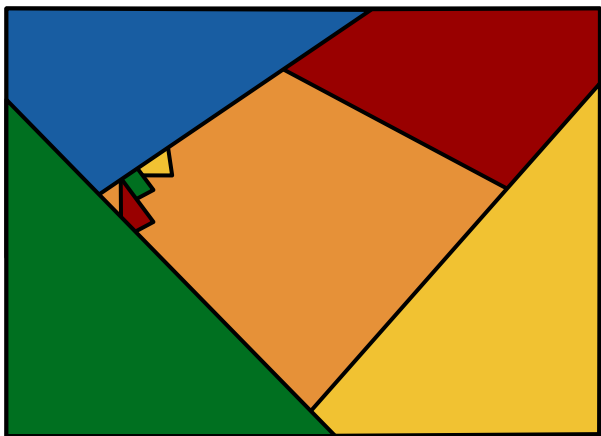
execution path
coverage of pa



\mathcal{T}

The Oracle: Testing an Analyzer

execution path
coverage of pa



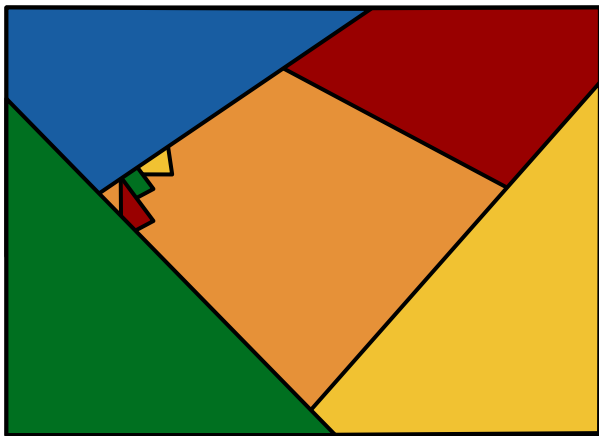
\mathcal{T}

mutate only parts
that affect pa

```
fnc collect(val, idx, obj) {  
  if (val >= this.threshold){  
    ... Query  
  }  
}  
Locations accessed by  
the analysis  
var dat = [5, 3, 9];  
dat.filter(collect, ctx);
```

The Oracle: Testing an Analyzer

execution path
coverage of pa



\mathcal{T}

mutate only parts
that affect pa

```
fnc collect(val, idx, obj) {  
  if (val >= this.threshold){  
    ... Query  
  }  
}  
Locations accessed by  
the analysis  
var dat = [5, 3, 9];  
dat.filter(collect, ctx);
```

select relevant
program mutations

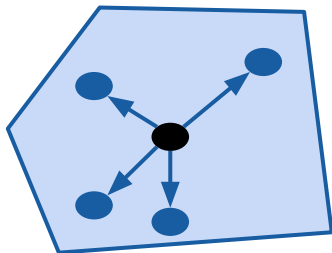
Modification via
Equivalence Modulo
Abstraction (EMA)

Modification via
Global Jumps

The Oracle: Testing an Analyzer

Modifications via Equivalence Modulo Abstraction (EMA)

Semantic preserving mutations



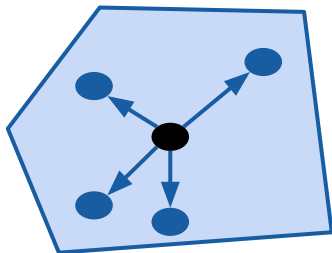
Adding dead code
Renaming variables
Renaming user defined functions
Side-effect free expressions

\mathcal{T}

The Oracle: Testing an Analyzer

Modifications via Equivalence Modulo Abstraction (EMA)

Semantic preserving mutations



Adding dead code
Renaming variables
Renaming user defined functions
Side-effect free expressions

labels y
can be reused

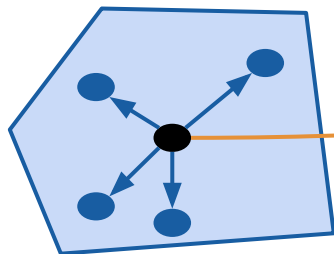
\mathcal{T}

The Oracle: Testing an Analyzer

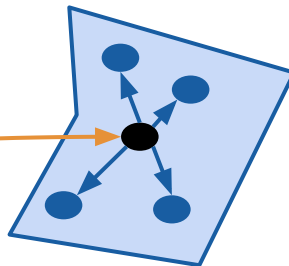
**Modifications via
Equivalence Modulo
Abstraction (EMA)**

**Modifications via
Global Jumps**

Semantic preserving mutations



Non-semantic preserving mutation



\mathcal{T}

Evaluation

ECMAScript (ECMA-262) Conformance Suite

15 675

Programs



Points-to Analysis

```
function collect(val, idx, obj) {  
  if (val >= this.threshold) { ... }  
}  
  
var dat = [5, 3, 9];  
dat.filter( collect, ctx );
```

A red arrow points from the `this` property access in the `if` statement to the `ctx` argument in the `filter` call.

Allocation Site Analysis

```
var obj = {a: 7};  
var arr = [1, 2, 3, 4];  
if (arr.slice(0, 2) == ... )  
var n = new Number(7);  
var obj2 = new Object(obj);  
try { ... } catch (err) { ... }
```

Blue boxes highlight the allocation sites for `obj`, `arr`, `n`, `obj2`, and `err`.

Approach Instantiation for Points-to Analysis

Input Dataset

$$\mathcal{D} = \{\langle x^j, y^j \rangle\}_{j=1}$$

$y \leftarrow$ **concrete object id**

*Language \mathcal{L}
for abstract
transformers*

$a \in \text{Actions} ::= \varepsilon \mid \text{Move}; a$

$\text{Move}_{\text{Core}} ::= \text{Up, Left, Right, DownFirst, DownLast, Top}$

$g \in \text{Guards} ::= \varepsilon \mid \text{Move}; g \mid \text{Write}; g$

$\text{WriteOp} ::= \text{WriteValue, WriteType, WritePos, HasLeftSibling, HasRightSibling, HasChild}$

Synthesis

$(\mathcal{H}, \sqsubseteq), \mathbf{a}, \boldsymbol{\gamma}$

semantic preserving mutations

Adding dead code

Renaming variables

Renaming user defined functions

Side-effect free expressions

non-semantic preserving mutations

Add method arguments

Add method parameters

Change program constants

Oracle

Learned Points-to Analysis

<i>Function Name</i>	<i>Dataset Size</i>	<i>Analysis Size</i>	<i>Counter-examples Found</i>
Function.prototype			
call()	26	97(18)	372
apply()	6	54(10)	182
Array.prototype			
map()	315	36(6)	64
some()	229	36(6)	82
forEach()	604	35(5)	177
every()	338	36(6)	31
filter()	408	38(6)	76
find()	53	36(6)	73
findIndex()	51	28(7)	96
Array			
from()	32	57(7)	160
JSON			
stringify()	18	9(2)	55



*rules missed by
Facebook Flow*

Average Learning Time 14 minutes (4 min synthesis, 10 min oracle)

Learned Allocation Site Analysis

134 721

training dataset size

905

counter-examples found

99

refinement iterations

3 hours

Synthesis time

7 hours

time to find counter-examples

Overview of Learned Analysis

```
if HasPrevNodeValue then  $\top$ 
elif WriteType == CallExpression then
  if Up WriteType == ExpressionStatement then
     $\top$  // return value not assigned
  else ...
elif WriteType == ArrayAccess then ...
elif WriteType == ObjectExp|ArrayExp|RegExp then
  NewAlloc // implicit constructors
elif WriteType == NewExpression then
  ... // explicit constructor
elif Up WriteType == AssignmentExpression
  if left hand side of the assignment then NoAlloc
  ...
```

Learning a Static Analyzer from Data

Learns practical abstract transformers
missed by existing state-of-the-art analyzers

Input Dataset
 $\mathcal{D} = \{\langle x^j, y^j \rangle\}_{j=1}$

Language \mathcal{L}
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